

Hints at the light scalar glueball

Wolfgang Ochs
MPI Munich

1. Expectations in QCD
2. Where to look for glue balls
3. Scalar meson spectrum
 - $q\bar{q}$ nonet
 - glue ball
4. Arguments for glueball

work with Peter Mukowski

Bern, S.S. 2006

Hints at the light scalar glueball

Wolfgang Ochs
MPI Munich

1. Expectations in QCD
2. Where to look for glue balls
3. Scalar meson spectrum
 - $q\bar{q}$ nonet
 - glue ball
4. Arguments for glueball

work with Peter Mikowski

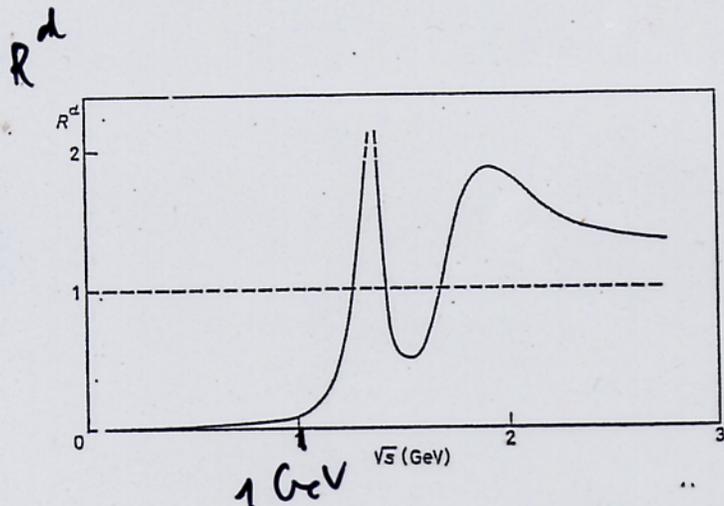
Bern, S.S. 2006

QCD predictions

H. Fritzsch & P. Minkowski
1975

Υ -RESONANCES, GLUONS AND THE ZWEIG RULE

Case A
resonating
gluons

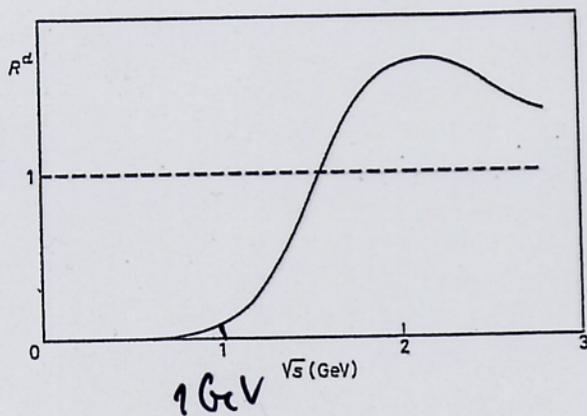


spectral fct.

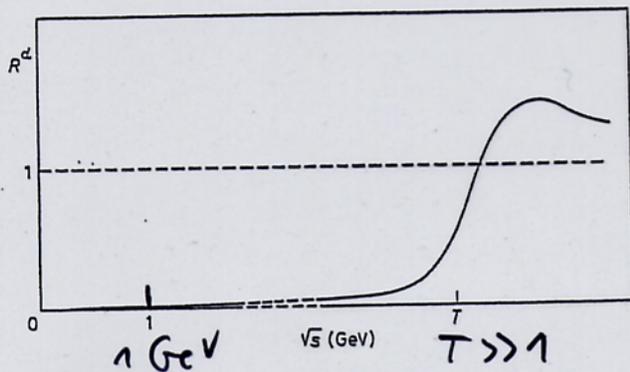
$$R^d(s) = \frac{\rho^d(s)}{\rho_0^d(s)}$$

$$\rightarrow 1 \quad (s \rightarrow \infty)$$

Case B
inconspicuous
gluons



Case C
delayed
saturation



$\rightarrow \sqrt{s}$

Today

Lattice QCD
QCD sum rules

lightest glueball $J^{PC} = 0^{++}$

(quenched approximation)

$M \sim 1.4 - 1.8 \text{ GeV}$
Bali 2003

$M \sim 1 \text{ GeV}$
 $M \sim 1.2 \text{ GeV}$

Navison
Forkel

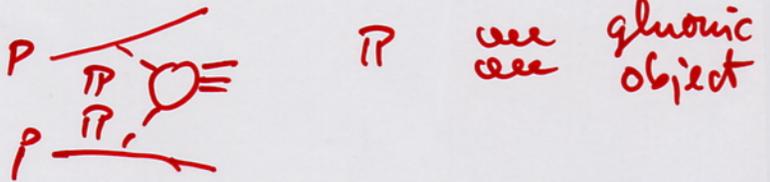
Where to look for glueballs?

"classic" proposals

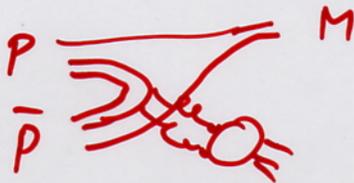
a) $J/\psi \rightarrow \gamma X$



b) $PP \rightarrow P X P$



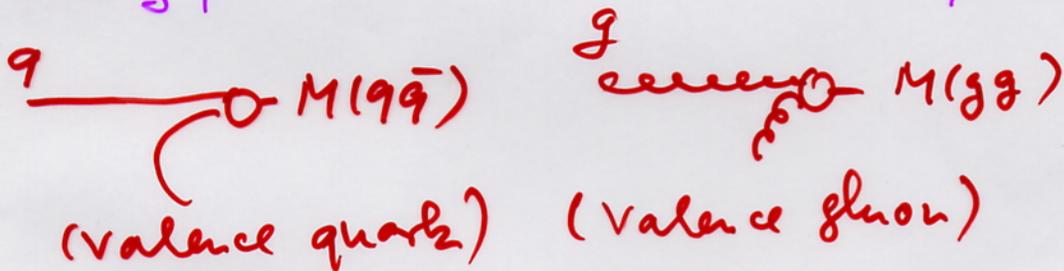
c) $P\bar{P} \rightarrow M X$
annihilation



more recent proposals

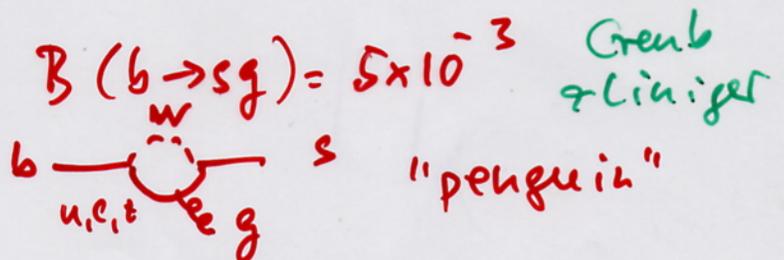
Minkowski, w.o.

a) leading part in gluon jet (rapidity gap)



b) B-decay

$B \rightarrow K gb$



problems 0^{++}

+ scalar meson spectrum difficult to disentangle
 $q\bar{q}$, $qq - \bar{q}\bar{q}$, gb

but additional component in gluon jets besides standard q, g + hadronization physics

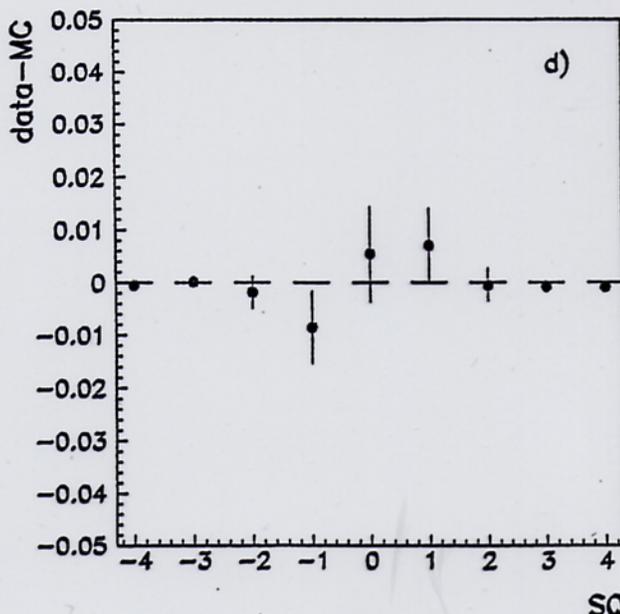
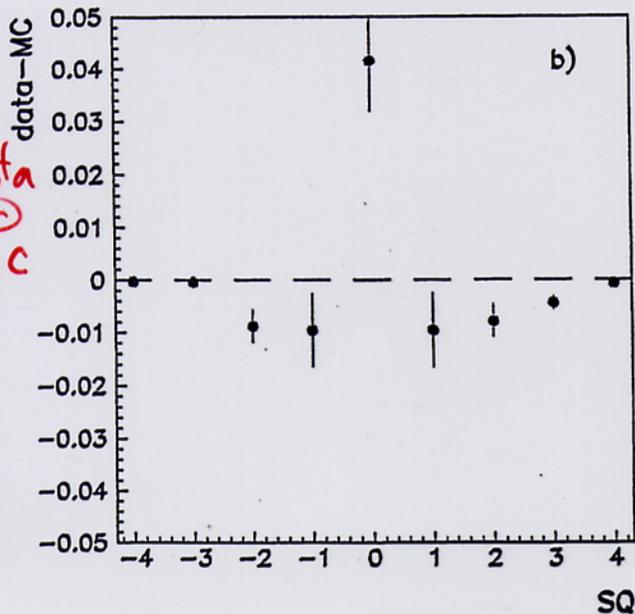
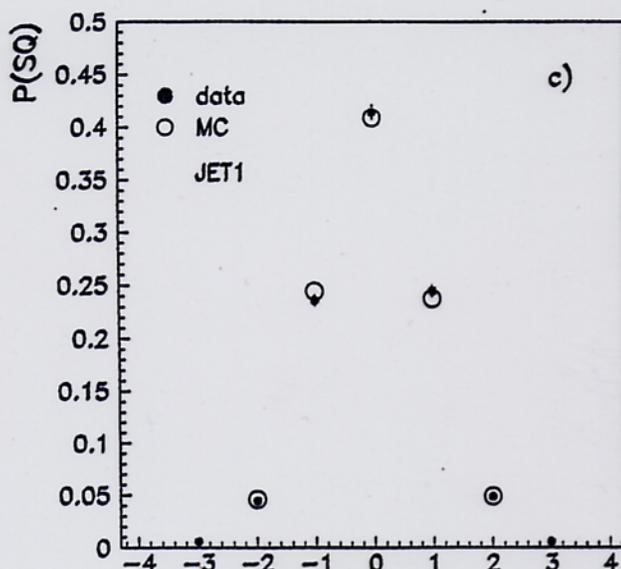
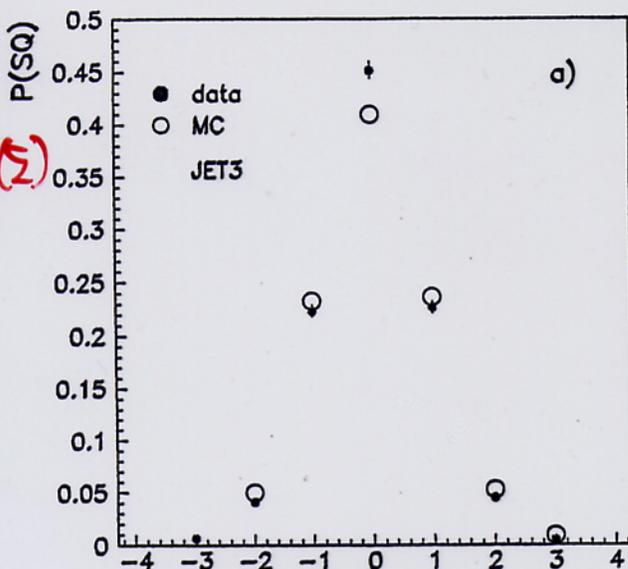
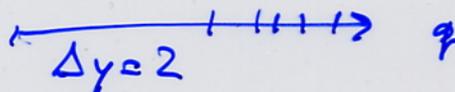
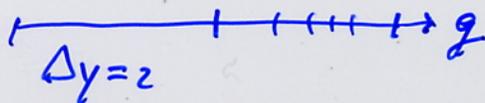
Delphi
OPAL
ALEPH

leading charge in

Delphi
hep-ph/0111408
(ISMD2001)

gluon jet

quark jet



$\sum_i Q_i$

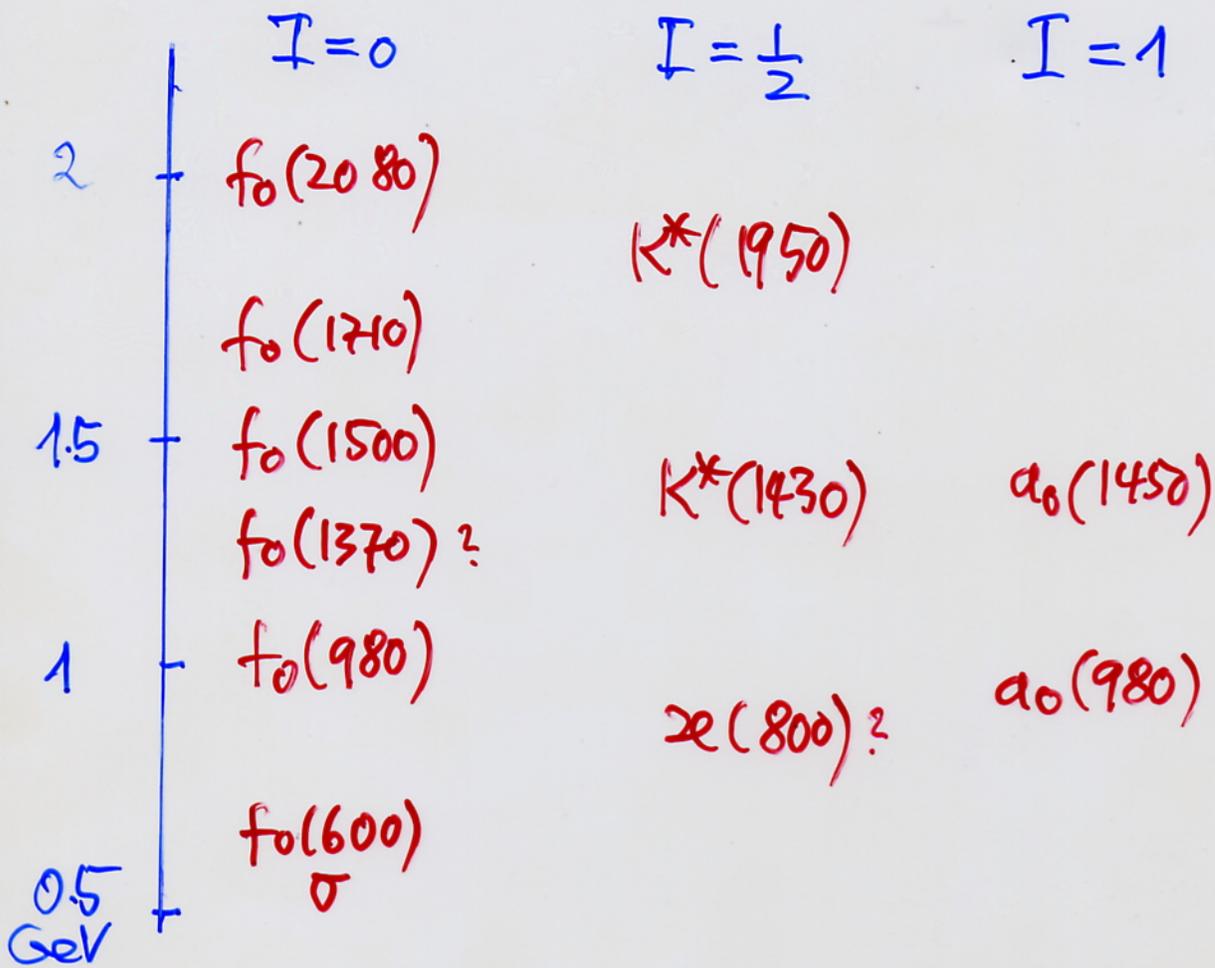
$\sum_i Q_i$

excess of charge $Q=0$
in gluon jet

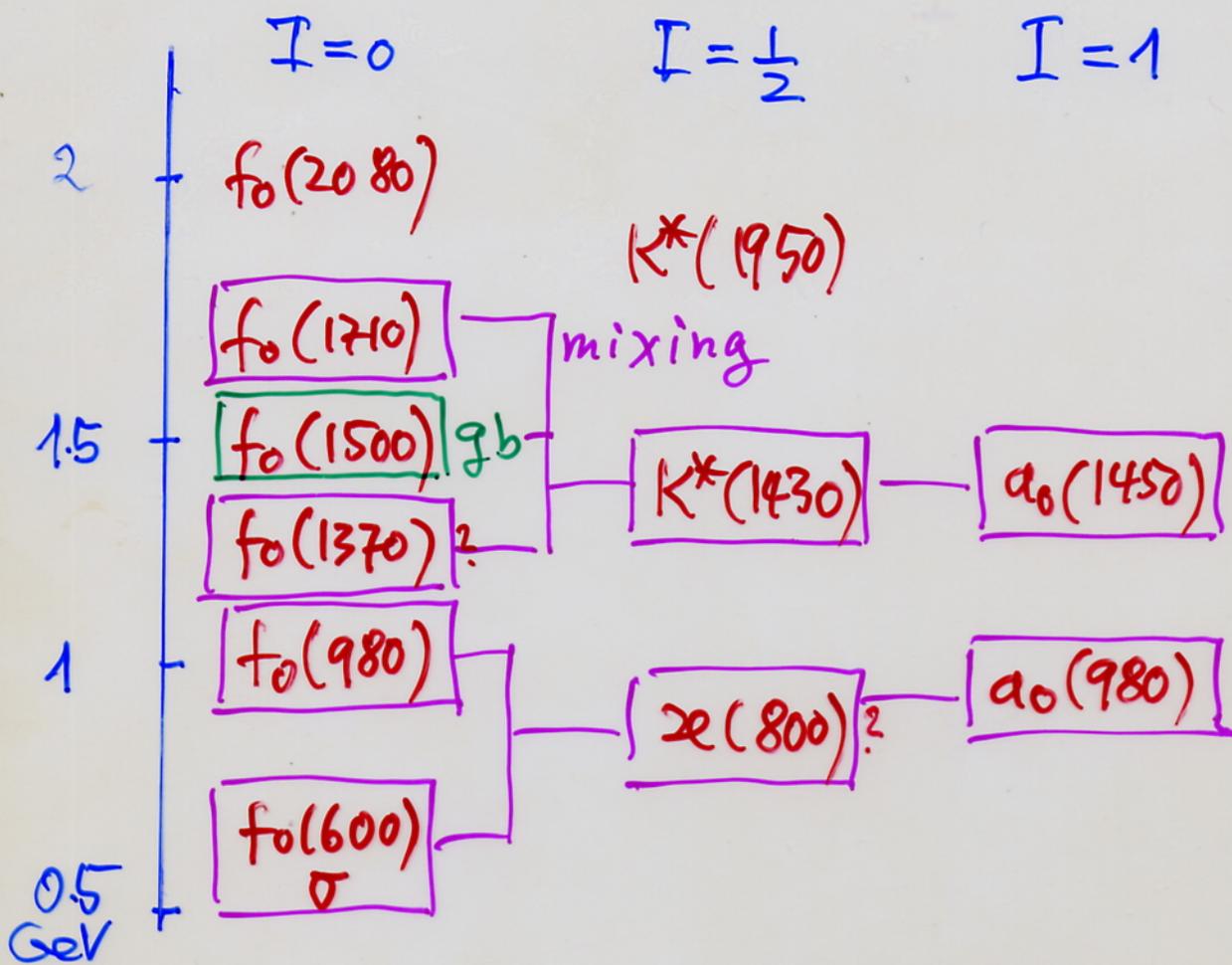
(with respect to jets string MC)



$J^{PC} = 0^{++}$ spectrum (PDG)



$J^{PC} = 0^{++}$ spectrum (PDG)



Two routes for classification

① 2 Multiplets below 1700 MeV

upper multiplet $L=1$ $q\bar{q}$ with $K^*(1430)$

0^{++} glueball expected around 1600 MeV
in quenched Lattice calculations

two isoscalars mix with glueball Anisler
? Cloe et al.

$\leftrightarrow f_0(1710), f_0(1500), f_0(1370)$

Lower multiplet

$q\bar{q}$, compact $qq-\bar{q}\bar{q}$, $K\bar{K}$ molecule

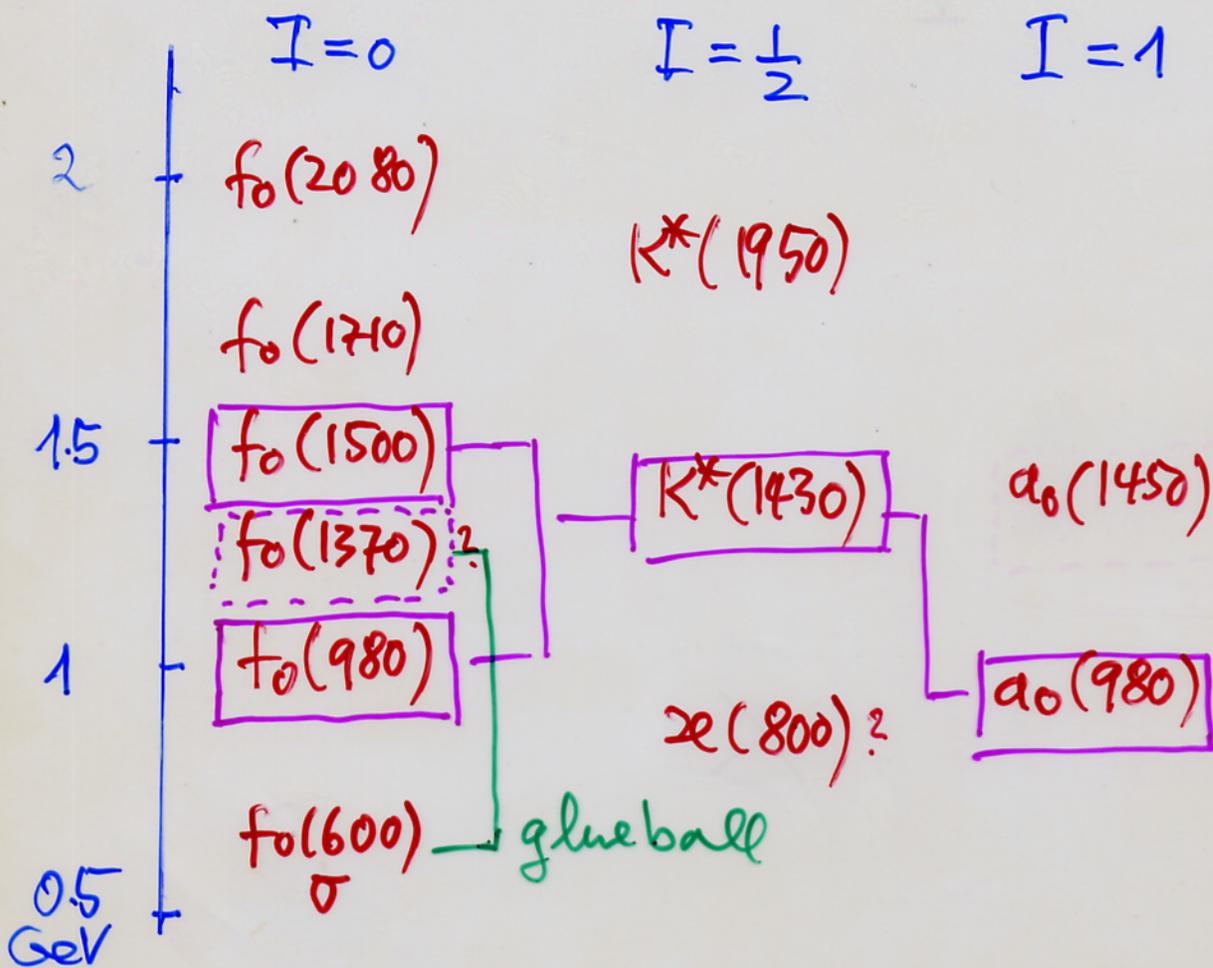
Jaffe, Adasov
Isgur Weinstein

low mass nonet $f_0(980), a_0(980), \sigma, \xi$

appears in theories of meson meson scattering
realizing chiral symmetry

review: Spanier, Tornqvist

$J^{PC} = 0^{++}$ spectrum (PDG)



② 1 Multiplet below 1700 MeV

- $q\bar{q}$ nonet with $f_0(980) - f_0(1500)$ mixed
like $\eta' - \eta$ Klemp, Metsch, et al.
Minkowski, W.O.
Anisovich, et al.
Narison
- broad glueball
around 1 GeV, $\Gamma \sim M$
differences in details but
- σ, ω not members of nonet
- $f_0(980)$ is the lightest $q\bar{q}$ scalar.

$$\underline{J^{PC} = 0^{++} \text{ howet}}$$

$f_0(1500)$

$K^*(1430)$

$f_0(980)$

$a_0(980)$

flavour mixing

1. $J/\psi \rightarrow \phi/\omega + f_0(980)$
2. Gell-Mann Okubo
3. $f_0, a_0 \rightarrow \gamma\gamma$
4. $f_0(980) \rightarrow K\bar{K}, \pi\pi$
5. $f_0(1500) \rightarrow \pi\pi, K\bar{K}, \eta\eta, \eta\eta'$ (?)

phases of $s\bar{s}$ component

6. $D_s \rightarrow f_0(980) / f_0(1500) + \pi$
7. $D \rightarrow \rho, f_0(980) + \pi$
8. $D_s \rightarrow \phi, f_0(980) + \pi$
9. $\text{Sign } f_0(980) \rightarrow K\bar{K} / \pi\pi$

future

$B \rightarrow K + \text{scalar}, K^* + \text{scalar}$

penguin dominance \rightarrow symmetry relations

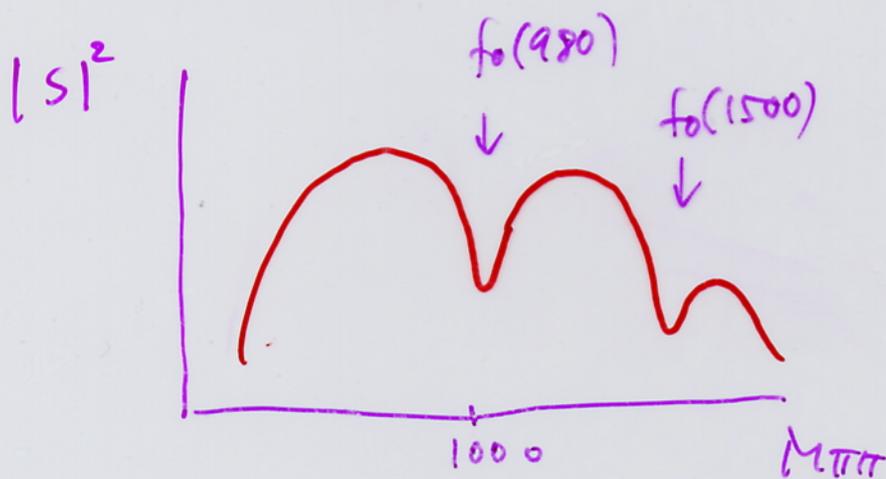
\rightarrow find $q\bar{q}$ howet

The lightest O^{++} glue ball

left over:

$f_0(1370)$
 $f_0(600) [\sigma]$ } gb (1000)

Minkowski
a-o.

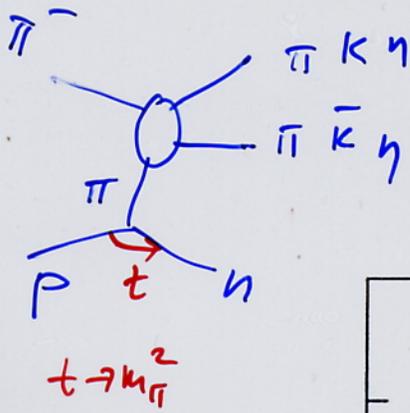


$\pi\pi \rightarrow \pi\pi$
"red dragon"

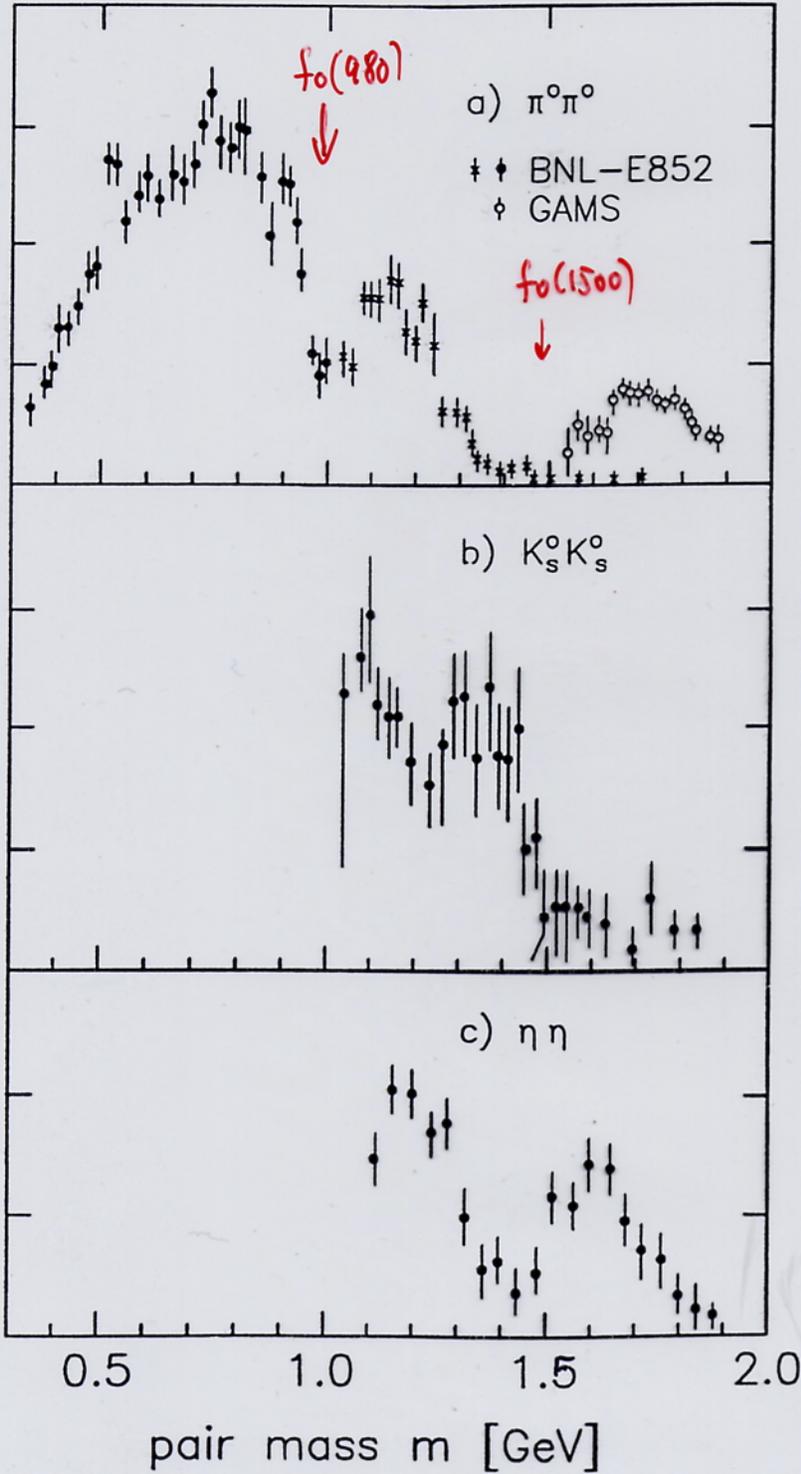


global fits yield broad state

S-wave in elastic and inelastic $\pi\pi$ scattering



$\frac{dn}{dm} (S_0 \text{-wave})$ [arbitrary units]



BNL
Grunke et al.
GAMS 196

"red dragon"

Etkin et al.
(similar to
Cohen et al.)

Biron et al.
GAMS

Interpretation of $\pi\pi$ S-wave

* low mass studies ($m_{\pi\pi} \lesssim 1.2$ GeV)

phase shifts rise slowly with mass

$$\delta_0^0 = 90^\circ \text{ at } m_{\pi\pi} \sim 900 \text{ MeV}$$

behaviour reproduced by σ -pole

* early history: Berkeley $\pi\pi$ (Protopopescu '73)

* recently: $D \rightarrow 3\pi$ (E791, FOCUS) $J/\psi \rightarrow \omega\pi\pi$ (BES)

* new "model independent" result

Caprini, Colangelo, Lentzky
2005

based on Roy eqs.

$$M_\sigma = 441^{+16}_{-8} \text{ MeV} \quad \Gamma_\sigma = 544^{+23}_{-18} \text{ MeV}$$

\rightarrow higher energies?

* high mass studies ($m_{\pi\pi} \lesssim 1800$ MeV)

all studies suggest broad state

* early history CERN-Munich (Hyams '75)

* coupled channel $\pi\pi, K\bar{K}$ (Estabrook '79)

* more channels Merga, Pennington,
Anisovich, Sarantsev

$$\text{mass } 1-1.5 \text{ GeV} \quad \Gamma \sim 0.5-1.0 \text{ GeV}$$

arguments for gluoball assignment

Anisovich, Sarantsev
Pivkouski w.o.

* Puzzle:

one amplitude circle
- 2 poles?

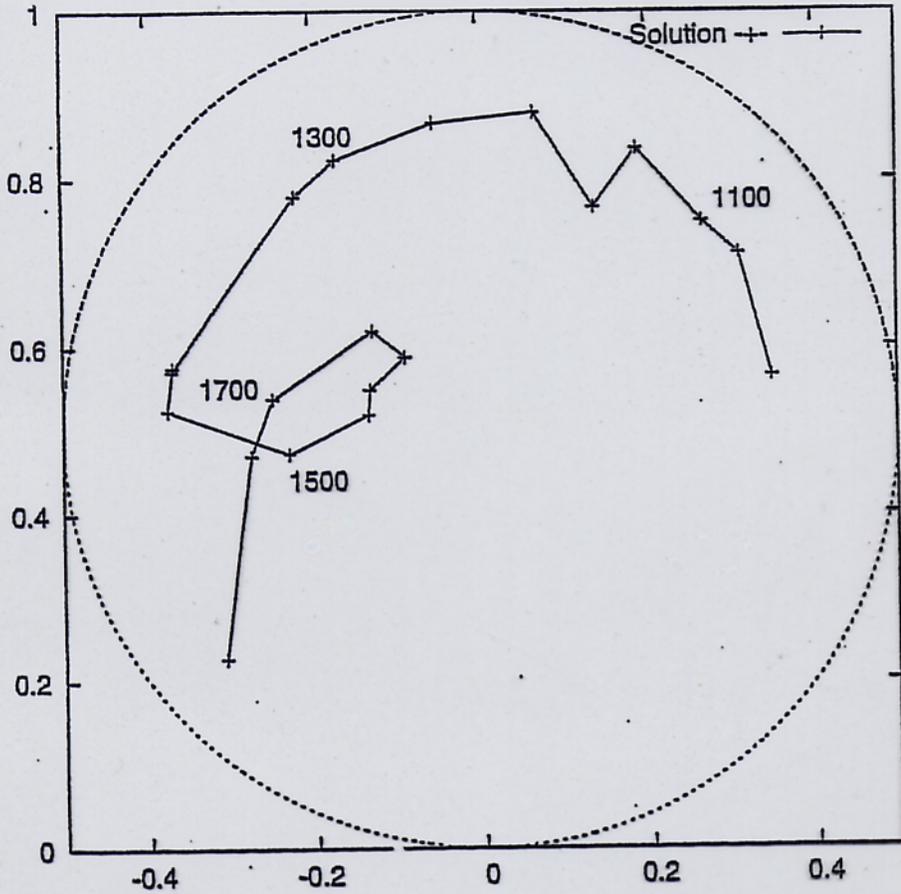
T_0^0

$I=0$

S-wave
sol. +-
preferred

μT_0^0

pi pi S wave amplitude in Argand diagram



$Re T_{00}$

$\mu > 1 \text{ GeV} :$ 4 solutions
2 excluded

unique up to $\mu \sim 1.4 \text{ GeV}$

Comparison of different analyses

CM 1

CM 2 [(- - -) = (- + -)]

CKM polarized target

Hyams '73

Hyams '75

Kaminski

-R. KAMIŃSKI, J. R. PELÁEZ AND F. J. YNDURÁIN-

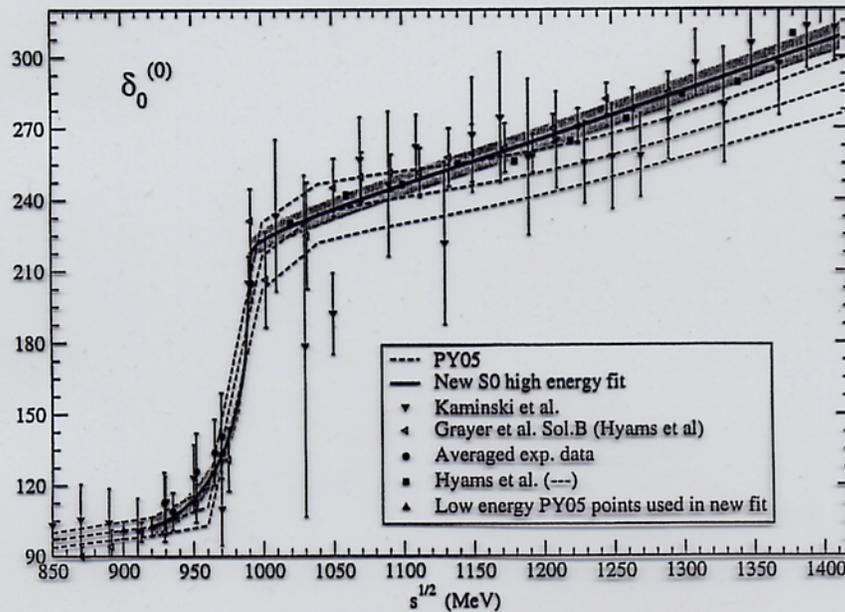


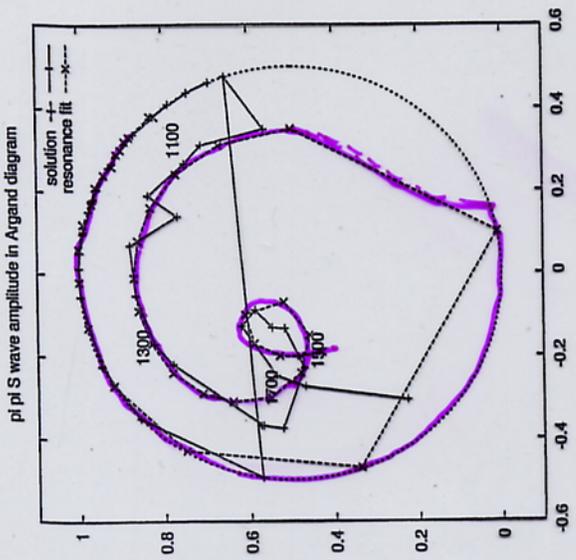
FIGURE 1. New fit to $\delta_0^{(0)}$ (solid line and dark area). The dashed lines stand for the phase shift from PY05 and its uncertainties. Note that the errors are now substantially smaller than in PY05, and that we now have a smooth matching with the PY05 low energy fit at 0.92 GeV.

sol. + - - , + + - excluded

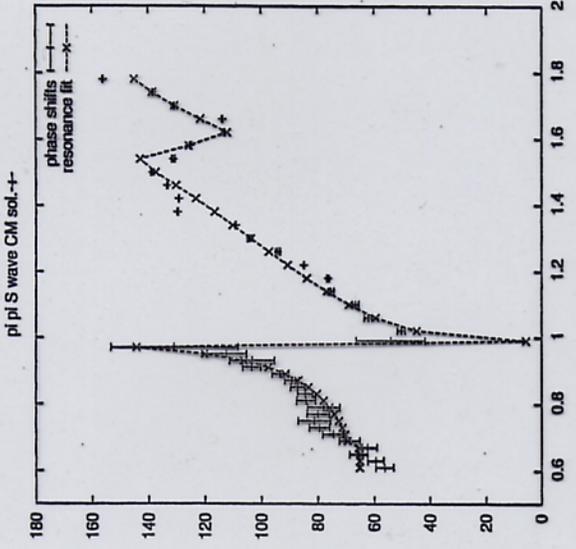
=> all solutions agree below $\sqrt{s} = 1.4 \text{ GeV}$

$\pi\pi$ S wave (preliminary) sol. -+-

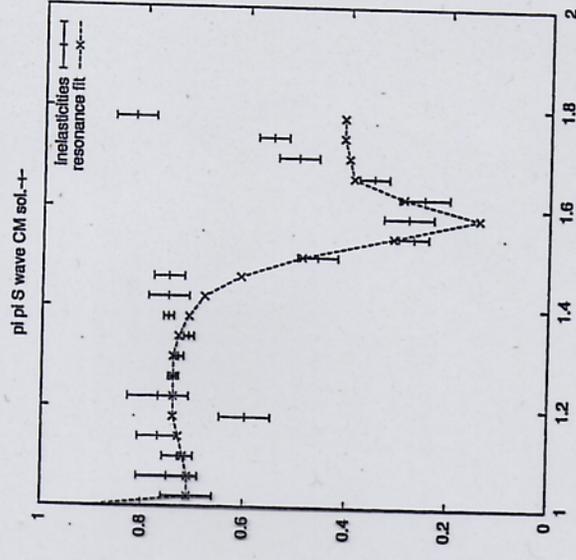
T_0



δ_0^0



η_0^0



$M_{\pi\pi} \rightarrow$

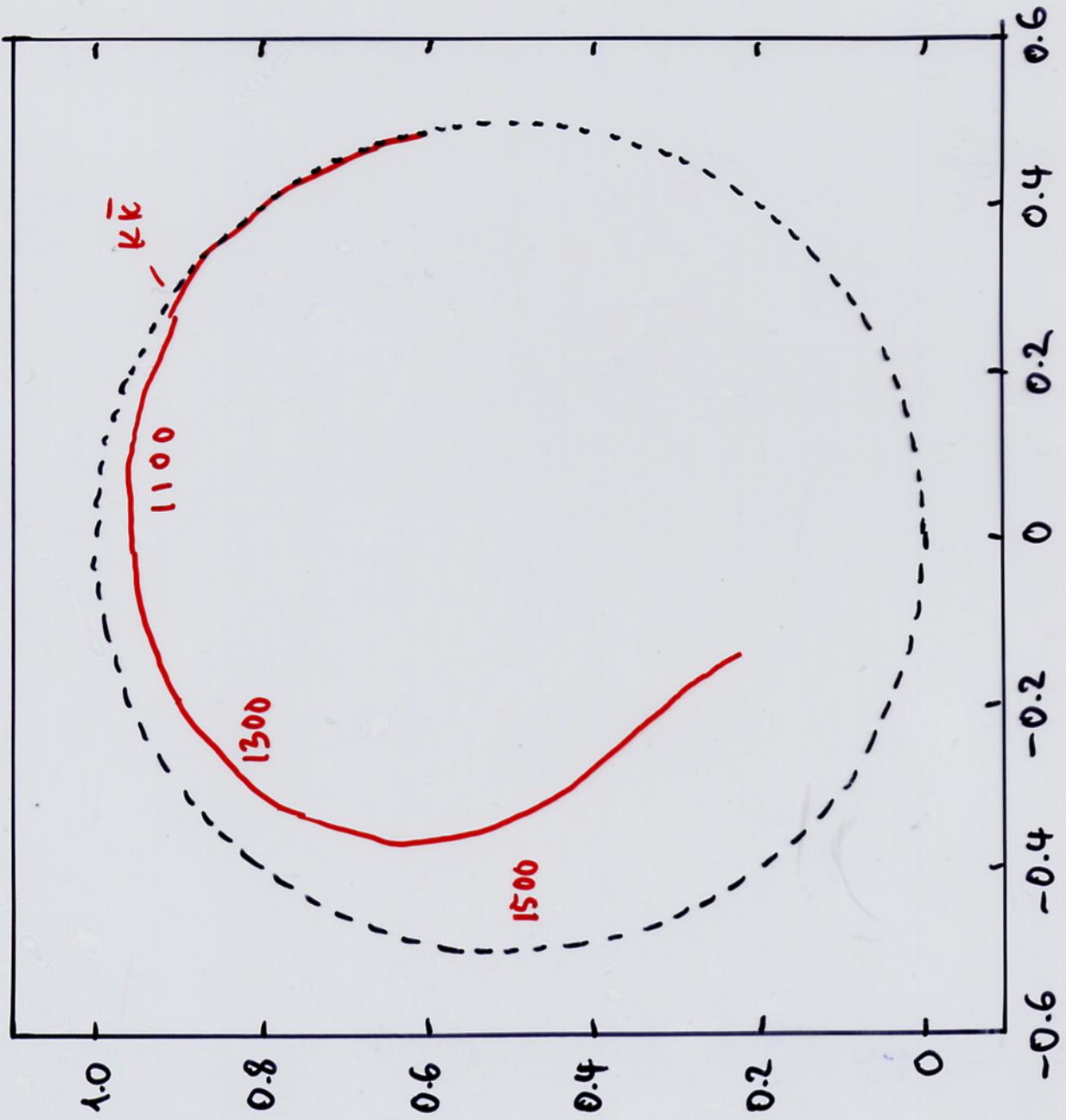
$$+ f_0(1500) e^{i\phi_2}$$

$$+ f_0(980) \cdot e^{i\phi_1}$$

$$T = f_0(1000) +$$

no $f_0(1370)$ included

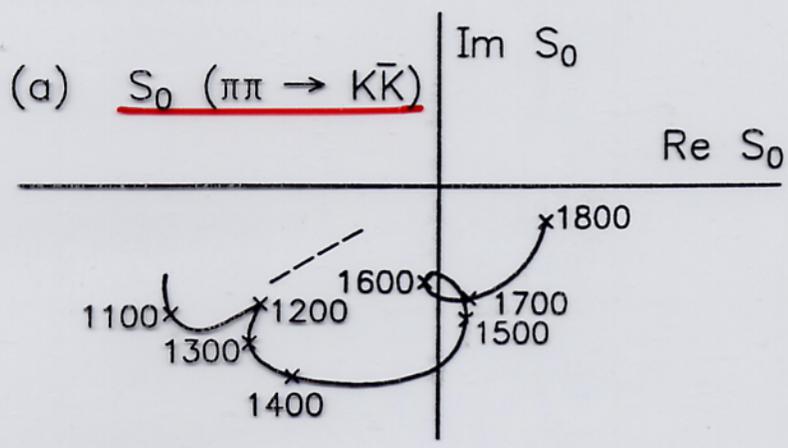
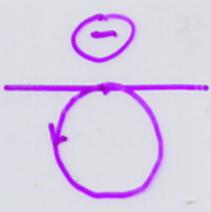
$\pi\pi$ Swave : "glue ball" component



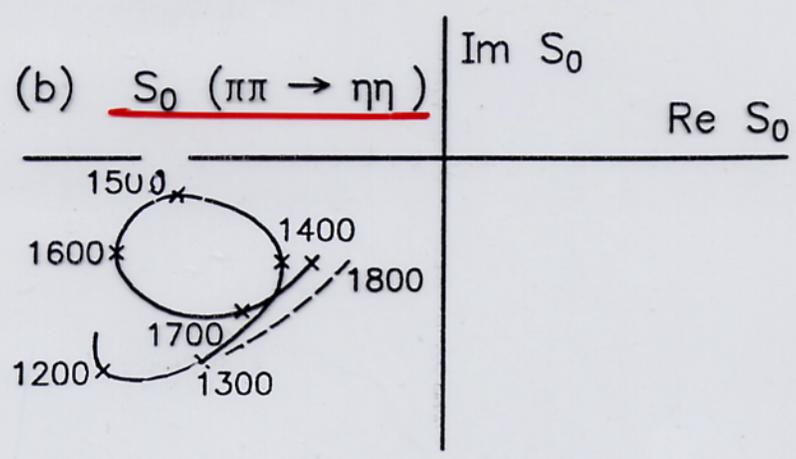
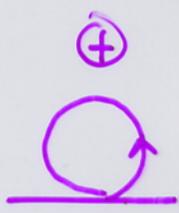
Relative signs of decay amplitudes

	$f_0(980)$	$f_0(1500)$	glueball
$K\bar{K}$	+	⊖	+
$\eta\eta$	+	⊕	+
$(u\bar{u} \quad d\bar{d} \quad s\bar{s})$	$(1 \ 1 \ 2)/\sqrt{6}$	$(1 \ 1 \ -1)/\sqrt{3}$	$(1 \ 1 \ 1)/\sqrt{3}$
$\pi\bar{\pi}$	+	⊕	+

Minkowski
w-o.
199 $f_0(1500)$



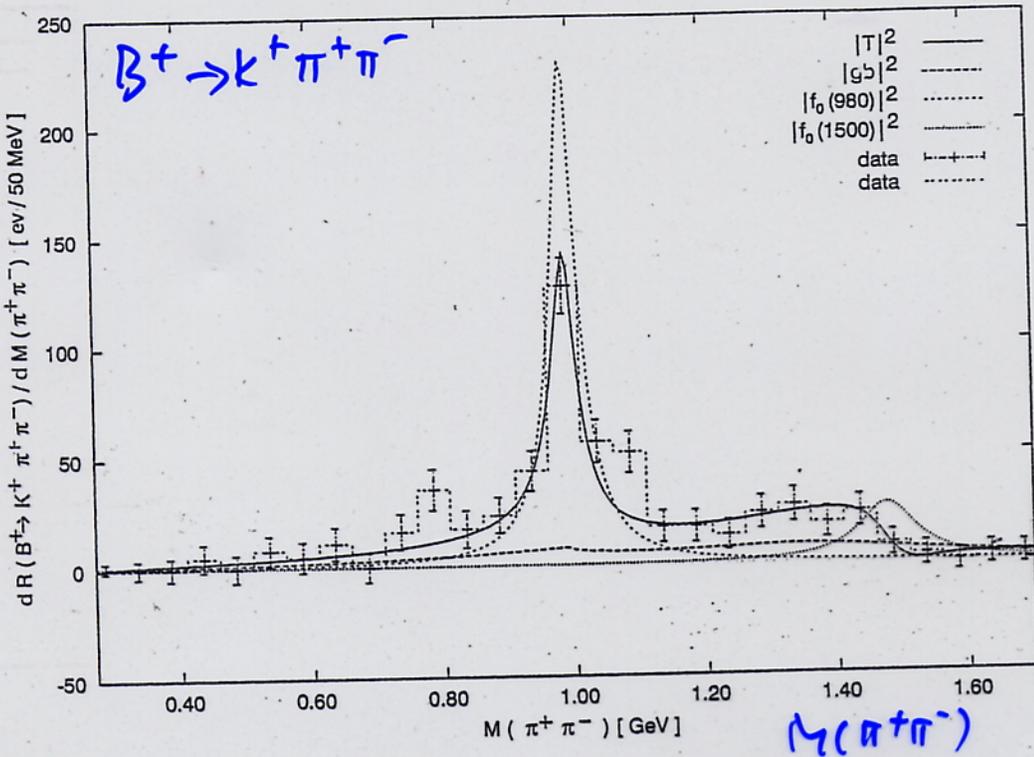
⊖ $s\bar{s}$



⊕ $h\bar{h}$

Amplitudes reconstructed from $|S|, |D|, \phi_{SD}$,
absolute phase: D wave Breit Wigner

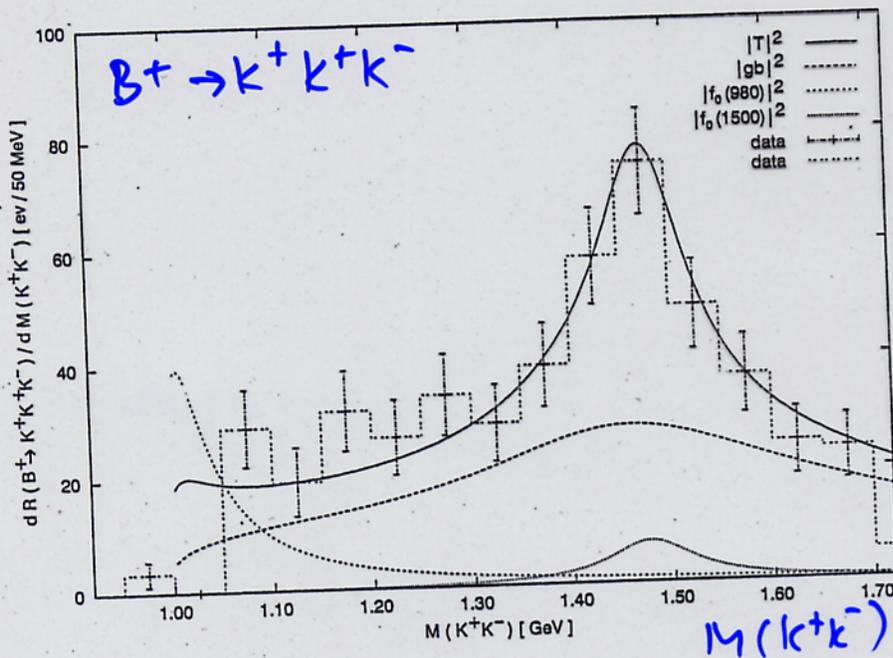
$X(1500)$ (BaBar) & $f_X(1500)$ (Belle) as $f_0(1500)$



Belle data
fits
Mikowski
ε W.O. 2004

bg - f0

$$\frac{\Gamma(K\bar{K})}{\Gamma(\pi\pi)} = 0.24$$



bg + f0

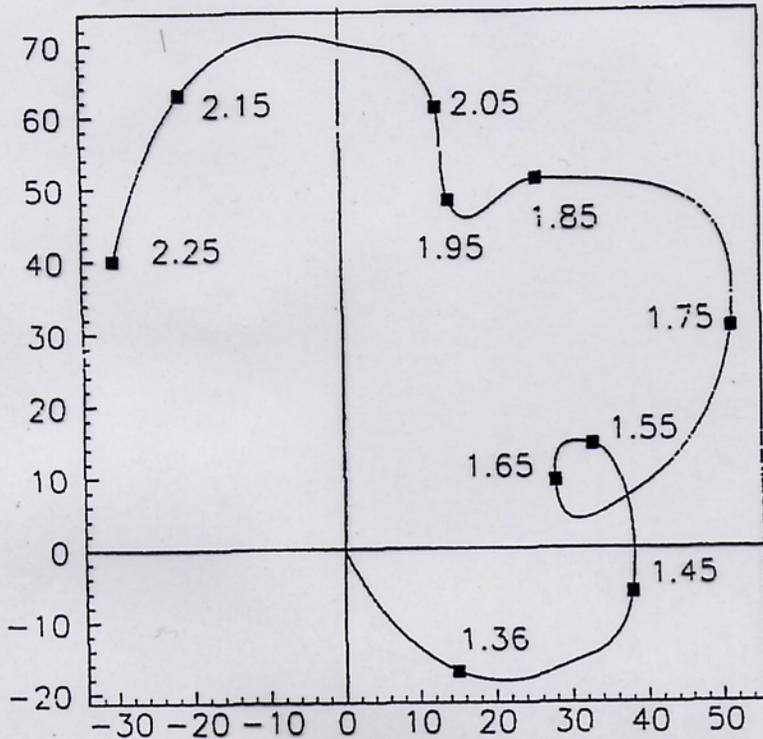
$$\frac{d\Gamma}{dm} = |c_1|^2 a^p |T_{gb} + c_2 T_{f_0} S_{gb} + c_3 T_{f_0'} S_{gb}|^2$$

$$a: gb, f_0, f_0' \quad T_a = m_a \Gamma_a / (m_a^2 - m^2 - i m_a \Gamma_a (1 + G_a(m)))$$

$$S_{gb} = e^{2i\delta_{bg}}; \quad T_{gb} = |T_{gb}| e^{i\delta_{bg}}$$

Analysis $\supset/4 \rightarrow \gamma(\pi^+\pi^-\pi^+\pi^-)$
 MARK III

D.V. Bugg et al. / Physics Letters B 353 (1995) 378-384



← $f_0(1500)$
 sign
 as in $\pi\bar{\pi} \rightarrow \pi\pi$
 $\rightarrow \eta\eta$

Fig. 3. The Argand diagram for the 0^+ scattering amplitude. $M(4\pi)$ is shown in GeV/c^2 .

Table 3

Changes ΔS in log likelihood when various components of the fit are dropped and remaining contributions are re-optimised

Contribution	ΔS
$f_2(1270) \rightarrow \rho\rho$	41.0
$\omega(1440) \rightarrow \rho\rho$	813.2
→ $f_0(1505) \rightarrow \sigma\sigma$	38.0
$f_0(1505) \rightarrow \rho\rho$	0.41; omitted
$f_2(1640) \rightarrow \sigma\sigma$	0.02; omitted
$f_2(1640) \rightarrow \rho\rho$	41.1
$f_2(1750) \rightarrow \sigma\sigma$	72.7
$f_2(1750) \rightarrow \rho\rho$	14.4
$f_0(2104) \rightarrow \sigma\sigma$	72.6
$f_0(2104) \rightarrow \rho\rho$	0.56; omitted
Background term	172.4

no $f_0(1370)$

Blue ball interpretation of " $f_0(1000)$ "

- partial wave amplitude in $\pi\pi \rightarrow \pi\pi$ 0^{++} describes circle: "left over state"

$$M \sim 1000 - 1400 \text{ MeV}$$

$$M \sim 500 - 1000 \text{ MeV}$$

- interference $f_0(1500)$ - gb in

$$\pi\pi \rightarrow \pi\pi, \eta\eta, K\bar{K}$$

$$B \rightarrow K(\pi\pi), K(K\bar{K})$$

- production in

$$J/\psi \rightarrow \gamma\pi\pi?, \gamma K\bar{K}_V, \gamma 4\pi_V$$

$$PP \rightarrow P(\pi\pi)P_V \text{ central}$$

$$P\bar{P} \rightarrow 3\pi_V$$

- suppression in $\gamma\gamma$ of $f_0(400-1200)$